

Definitions Matter: Reconciling Differential and Adversarial Privacy

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Example: AOL Search Data Fiasco



[August 4th 2006]

User Id	Search Query
4417749	“landscapers in Lilburn, GA”
4417749	“people with last name Arnold”
4417749	“numb fingers”
4417749	“dog that urinates on everything”

↓
Anonymized Search Logs for Research

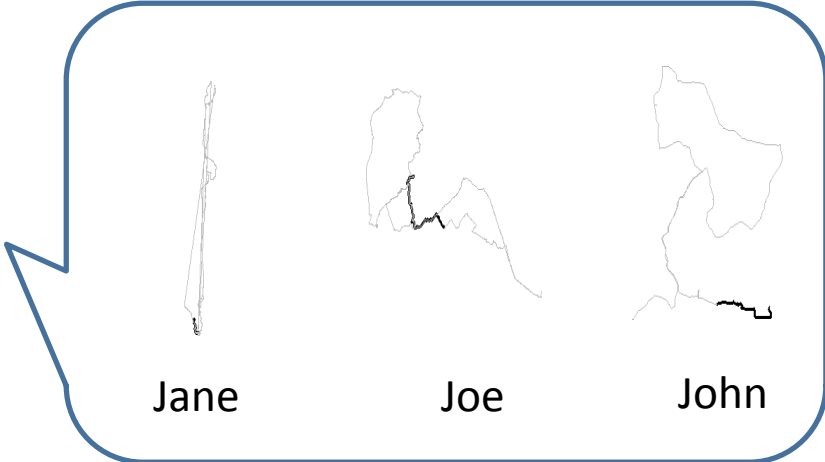
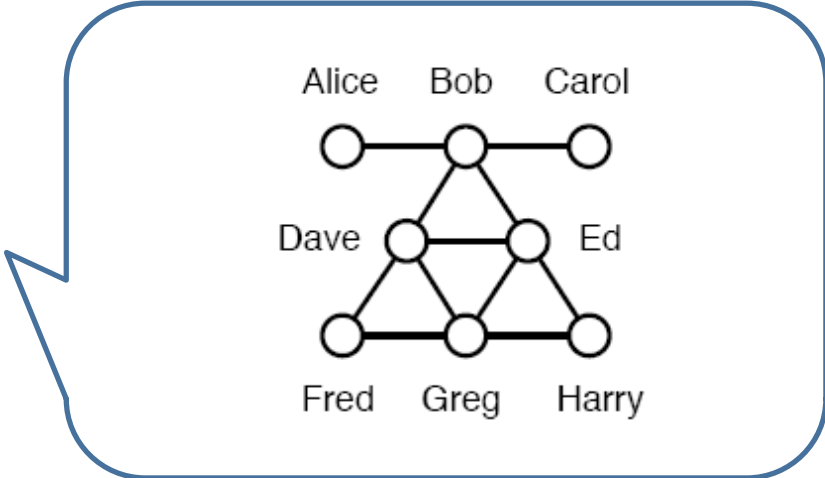
End user (Thelma): opt-in/opt-out decision

Data owner (CIO): publish/no-publish decision

Needed: formal privacy guarantees

Other Examples of Private Data

facebook

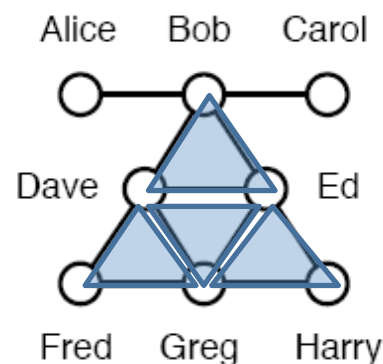


Other Examples of Private Data

Understand social trends

How many triangles in the graph?

Deny: *Who are Bob's friends?*



No known techniques with privacy guarantees !

Analyze traffic & congestion

How many drivers take route I-90?

Deny: *Where does Joe go after work?*



Jane

Joe

John

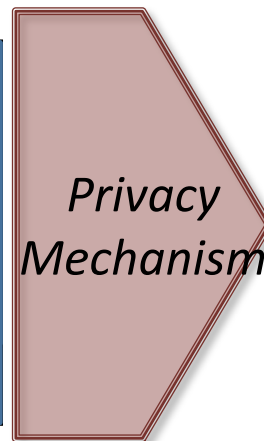
Outline

- Background: Privacy definitions
- Central result: Differential vs. Adversarial privacy
- Applications: New techniques with formal privacy
- Conclusions

Background: Differential privacy [Dwork 06]

State-of-the-art privacy definition

Name	Age	Zip	Disease
John	15	98104	Flu
....
Smith	27	98105	Cancer
Alice	11	98105	Flu



Possible perturbed answers:

163 prob = ~~p_1~~ p_1'
175 prob = ~~p_2~~ p_2'
.....

Query: ***count # of flu patients with age < 10***

Current correct answer = **156**

New correct answer = **157**

Differential Privacy [Dwork 06] Output probabilities change very little with addition/removal of a single tuple

Background: Differential privacy [Dwork 06]

max change in query answer on adding/removing a single tuple

Standard Algorithm [Dwork et. al. 06]

- Add random noise according to **query sensitivity**

Example:

SELECT-COUNT-WHERE queries:

'# of flu patients with age < 10'

Answer can change by at most 1

Query sensitivity is 1

Small noise required

Name	Age	Zip	Disease
John	15	98104	Flu
.....
Smith	27	98105	Cancer
Alice	11	98105	Flu

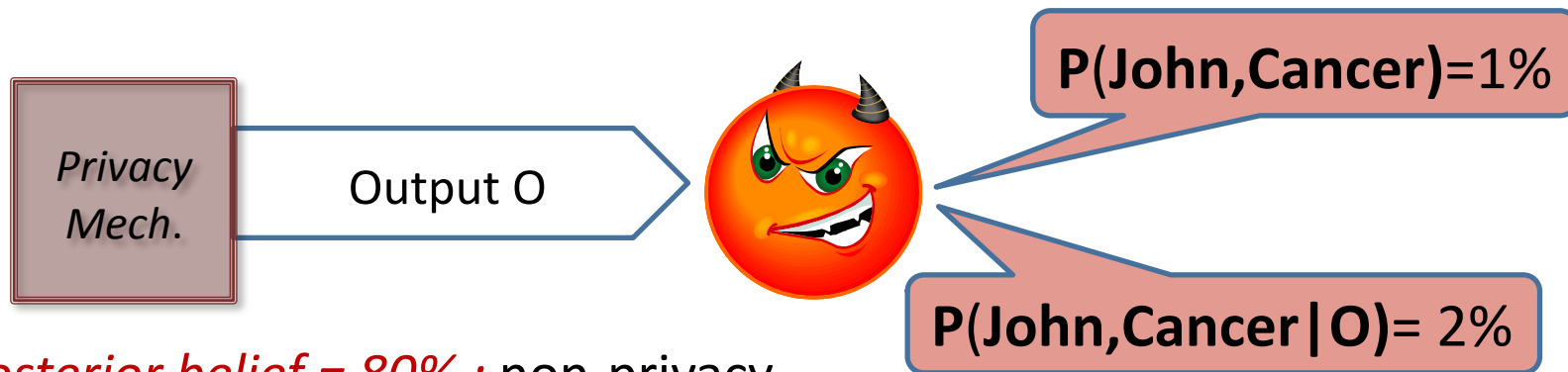
Summary of Differential Privacy

- Designed for the end-user
 - Opt-in/opt-out decision
 - Property of the security mechanism, not of attackers
- Simple privacy mechanism based on query sensitivity

Background: Adversarial Privacy

Models the attacker explicitly

Prior belief

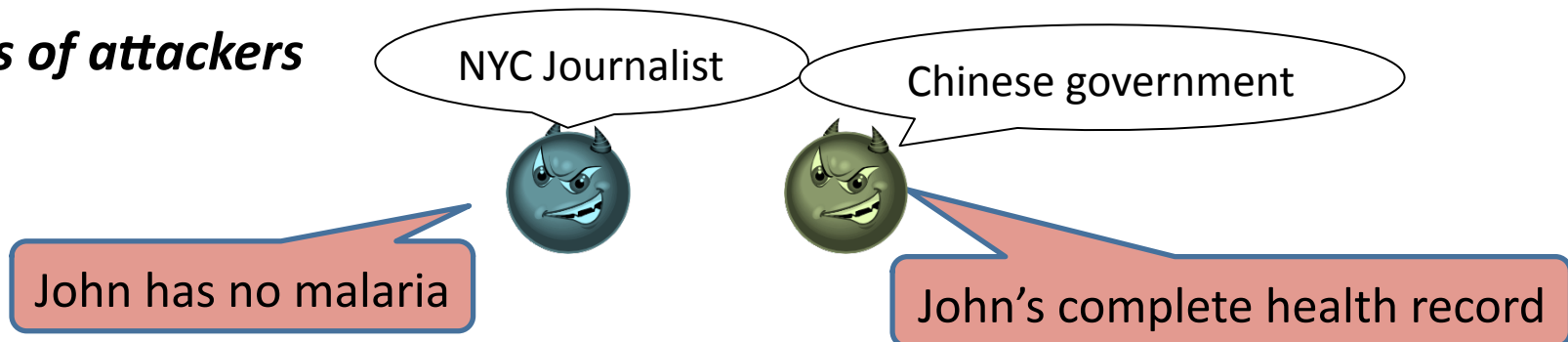


Posterior belief = 80% : non-privacy

Posterior belief = 1.2% : privacy

Posterior belief

Class of attackers



Adversarial privacy [Evfimievski 02] For all attackers in a **class**, his knowledge changes little after learning the query's answer

Summary of Adversarial Privacy

- Designed for the data owner
 - Publish / don't publish decision
 - Stated in terms of an attacker, not the privacy mechanism
 - Applies equally well to group secrets

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Differential vs. Adversarial Privacy

Against which class of attackers does differential privacy protect?

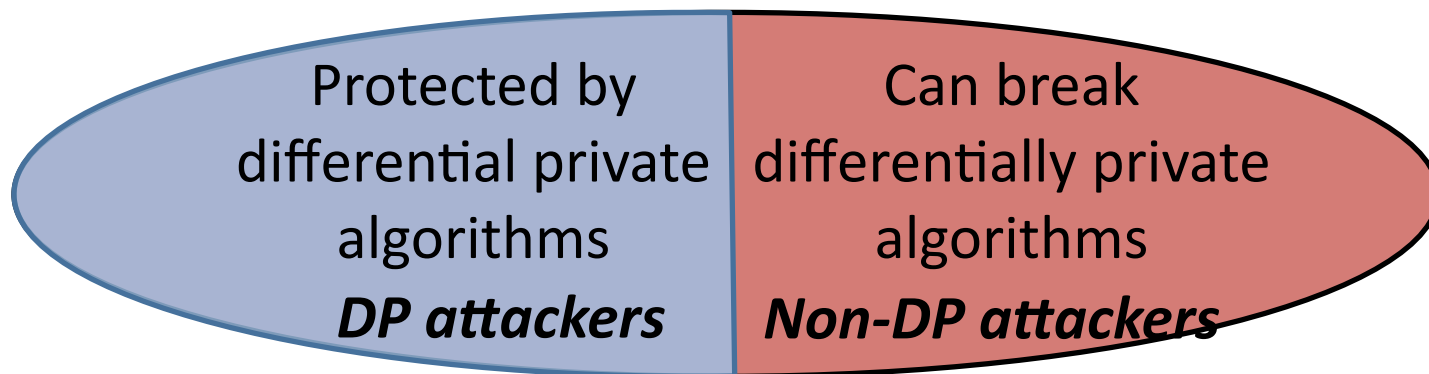
Differential vs. Adversarial Privacy

Against which class of attackers does differential privacy protect?

Equivalence Result [Rastogi. et. al. 09]

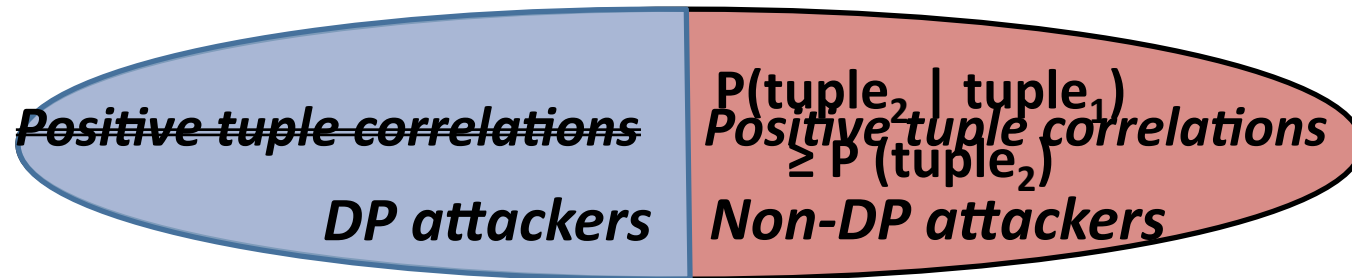
Characterized the class of **DP attackers** for which*:

adversarial privacy against **DP attackers** = **differential privacy**



All possible attackers

***DP & Non-DP* Attackers**

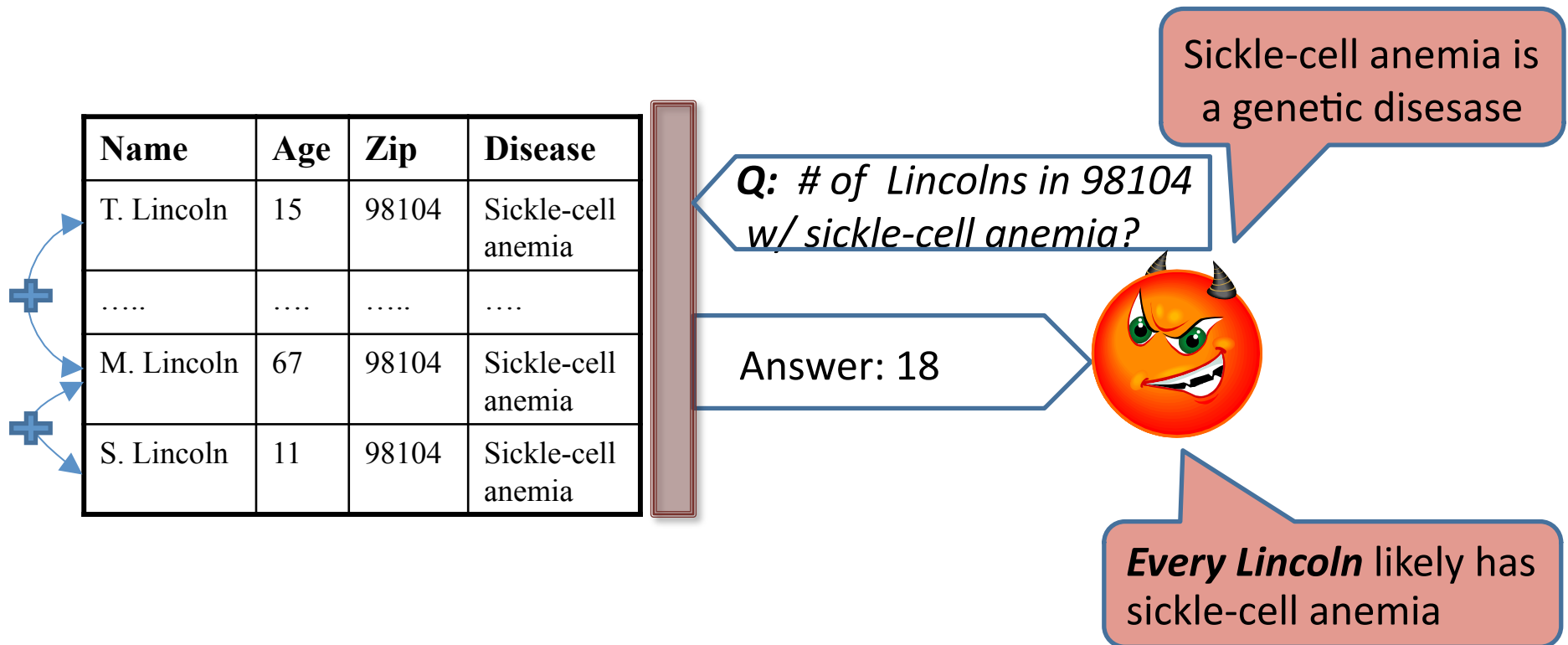


Formal definition of DP attackers

An attacker with prior belief distribution \mathbf{P} is ***DP*** iff:

1. \mathbf{P} is *log-submodular*
2. Every marginalization of \mathbf{P} is also *log-submodular*
3. \mathbf{P} is *planar*: exists n , $P(\text{DB})=0$ if $|\text{DB}| \neq n$

Non-DP Attackers: Positive Tuple Correlations

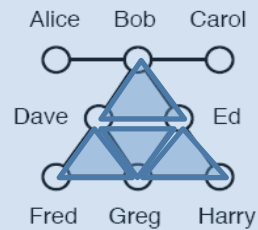


- In differential privacy, noise added according to query sensitivity
- That noise insufficient to hide the presence or absence of 20 tuples

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Applications: Analysis of Social Networks



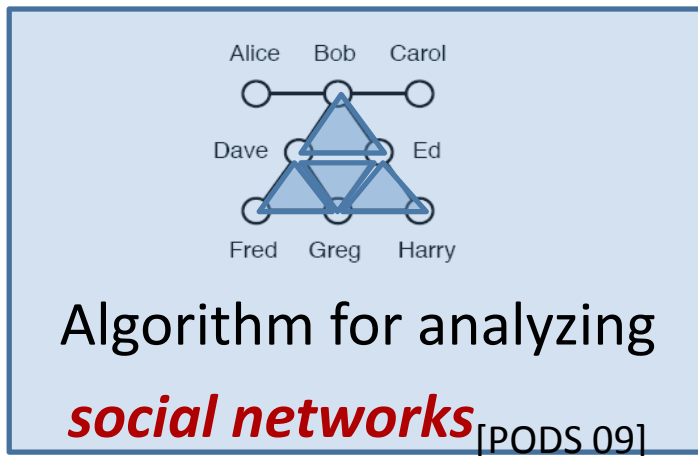
Algorithm for analyzing
social networks [PODS 09]



Algorithm for analyzing
time-series data [SIGMOD 10]

Central Result [PODS 09]: Connection between
Differential Privacy [Dwork 06] & ***Adversarial Privacy*** [Evfimievski 02]

Applications: Analysis of Social Networks



Error in response
for Differential Privacy

Common Graph Queries	Error
# of triangles	$\Theta(n)$
# of paths of length 2	$\Theta(n)$
# of cycles of length i	$\Theta(n^{i-2})$
# of nodes at dist. i	$\Theta(n)$
# of cliques of size i	$\Theta(n^{i-2})$

Motif Analysis [Newman 03]

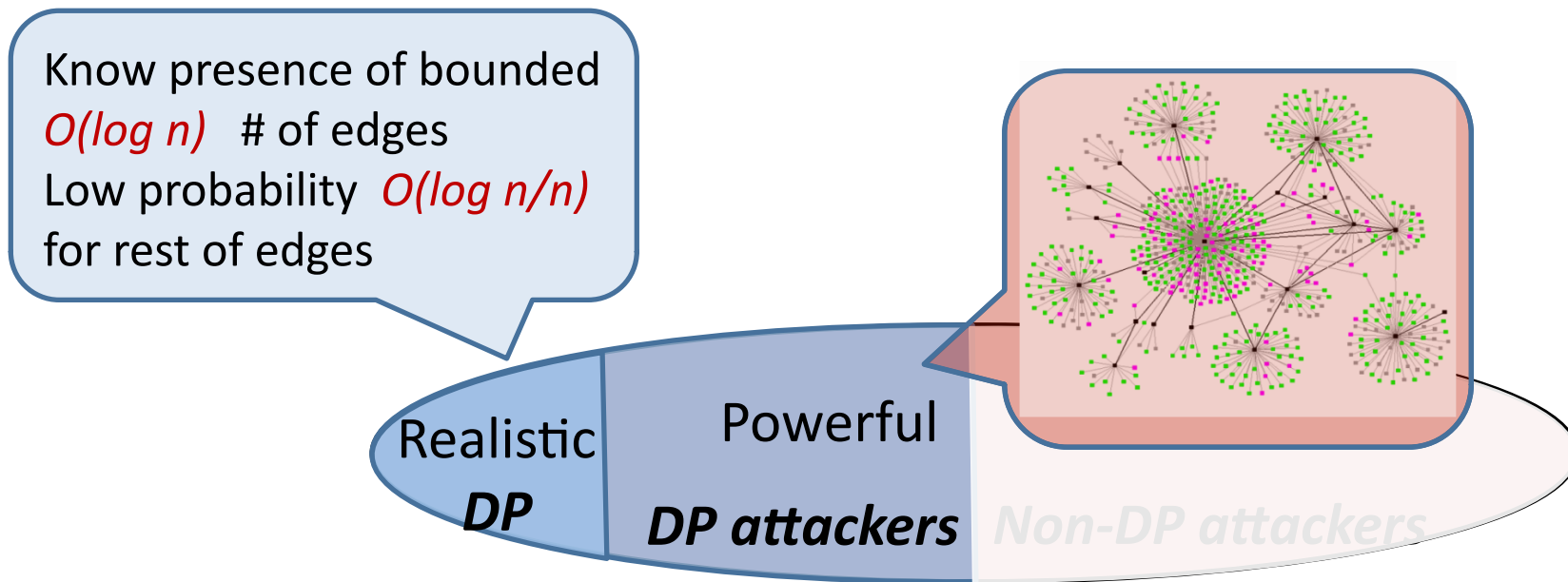
To understand the structure
of the social network graph

Differential privacy adds too much noise

DP is too strong for social networks.

Relaxing Differential Privacy

- Use its connection with adversarial privacy



adversarial privacy against **realistic DP** attackers

Our Algorithm

Modification of the standard differentially private algorithm

Standard Algorithm [Dwork et. al. 06]

- Add random noise according to ***query sensitivity***

- Random noise has an expected error of Θ (query sensitivity)

Example '*# of triangles*': query sensitivity = $n-2$
expected error = $\Theta(n)$

Our Algorithm

Modification of the standard differentially private algorithm

Expected change in query answer on adding/removing a single tuple

Our Algorithm [Rastogi et. al. 09]

- Return completely random answer with negligible probability
- Otherwise add random noise according to **adversarial sensitivity**

Example ‘# of triangles’: **adversarial sensitivity** = $O(\log^2 n)$
expected error = $O(\log^2 n)$

We bound **adversarial sensitivity** for a large class of queries
Proof based on new concentration results

Examples for Improved utility

Graph Query	Standard [Dwork06]	Ours [R. et. al. 09]
# of triangles	$\Theta(n)$	$\Theta(\log^2 n)$
# of 2-length paths	$\Theta(n)$	$\Theta(\log n)$
# of i-node cycles	$\Theta(n^{i-2})$	$\Theta(\log^{i-1} n)$
# of nodes at dist. i from a node v	$\Theta(n)$	$\Theta(\log^{i-1} n)$
# of i-node cliques	$\Theta(n^{i-2})$	$\Theta(\log^{i^2} n)$
# of conn. subgraphs of i nodes & j edges	$\Theta(n^{i-2})$	$\Theta(\log^{i-1} n)$

- **Standard** satisfies differential privacy = adversarial privacy against **all DP** attackers
- **Ours** satisfies adversarial privacy against only **realistic DP** attackers

The Class of Queries (Details....)

- Answer **count(q)** where $q :- R_1, R_2, \dots$

$$\text{Density}(q) = |\text{Atoms}(q)| / |\text{Vars}(q)|$$

Definition q is dense, if $\text{Density}(h(q)) \geq 1$, for all homomorphism h

The **derivative** of q is:

$\partial(q(R_i))$ = replace R_i with constants, then remove R_i

Definition q is stable if for all $k \geq 1$, $\partial^k(q)$ is dense

Theorem Adversarial sensitivity is bounded
for all stable queries and “realistic” DP adversaries

Summary

- Differential privacy not possible for join queries
- Adversarial privacy possible against “relaxed DP” adversary for all “stable” queries

Applications: Analysis of Time-Series Data

[Rastogi & Nath: SIGMOD 2010]

Alice Bob Carol
Dave Ed
Fred Greg Harry

Algorithm for analyzing
social networks [PODS 09]

Algorithm for analyzing
time-series data [SIGMOD 10]

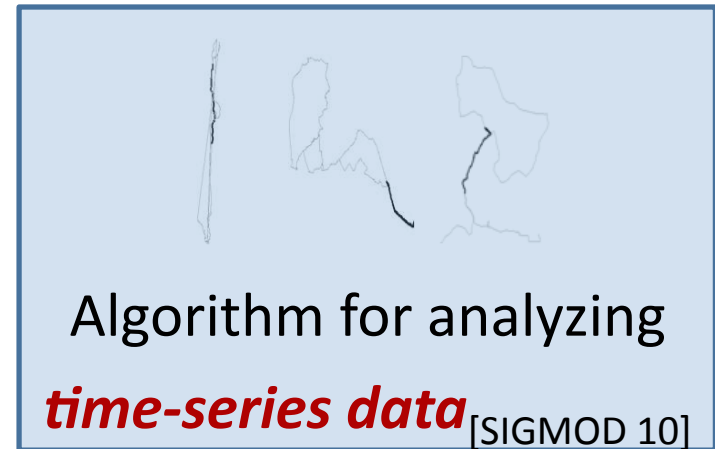
Equivalence Result [PODS 09]: Connects
Differential Privacy [Dwork 06] & ***Adversarial Privacy*** [Evfimievski 02]

Applications: Analysis of Time-Series Data [Rastogi & Nath: SIGMOD 2010]

Example: GPS traces

Name	Age	Location	Time
Alice	25	Dreese Labs	5 PM
Alice	25	Scott Labs	5:02 PM
Alice	25	Smith Labs	5:03 PM
Bob	32	Dreese Labs	5:35 PM

Lots of positive correlations!



**Differential privacy does not protect
against positive correlations**

Differential privacy too weak for time-series data!

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Conclusion

- Formal privacy guarantees required
- Differential privacy:
 - Opt-in / opt-out decision for end user
 - Property of privacy mechanism
- Adversarial privacy:
 - Publish / no-publish decision for data owner
 - Property of the class of attackers
- Fundamental equivalence theorem for *DP attackers*
- Applications to:
 - Analysis of Social Networks
 - Analysis of time-series data

Thank You!